

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
TOTAL	



General Certificate of Education  
Advanced Subsidiary Examination  
January 2012

# Mathematics

# MPC2

## Unit Pure Core 2

Friday 13 January 2012 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

### Time allowed

- 1 hour 30 minutes

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

### Advice

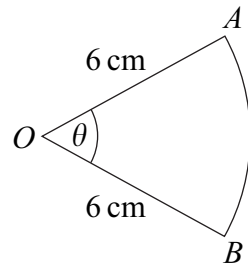
- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J A N 1 2 M P C 2 0 1

Answer **all** questions in the spaces provided.

- 1** The diagram shows a sector  $OAB$  of a circle with centre  $O$  and radius 6 cm.



The angle between the radii  $OA$  and  $OB$  is  $\theta$  radians.

The area of the sector  $OAB$  is  $21.6 \text{ cm}^2$ .

- (a)** Find the value of  $\theta$ . *(2 marks)*
- (b)** Find the length of the arc  $AB$ . *(2 marks)*

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- 2 (a)** Use the trapezium rule with five ordinates (four strips) to find an approximate value for

$$\int_0^4 \frac{2^x}{x+1} dx$$

giving your answer to three significant figures.

(4 marks)

- (b)** State how you could obtain a better approximation to the value of the integral using the trapezium rule.

(1 mark)

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**3 (a)** Write  $\sqrt[4]{x^3}$  in the form  $x^k$ . (1 mark)

**(b)** Write  $\frac{1-x^2}{\sqrt[4]{x^3}}$  in the form  $x^p - x^q$ . (2 marks)

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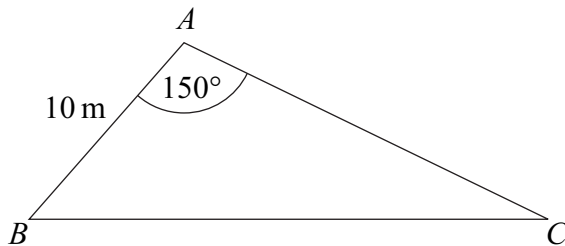
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**4** The triangle  $ABC$ , shown in the diagram, is such that  $AB$  is 10 metres and angle  $BAC$  is  $150^\circ$ .



The area of triangle  $ABC$  is  $40 \text{ m}^2$ .

- (a) Show that the length of  $AC$  is 16 metres. (2 marks)
- (b) Calculate the length of  $BC$ , giving your answer, in metres, to two decimal places. (3 marks)
- (c) Calculate the smallest angle of triangle  $ABC$ , giving your answer to the nearest  $0.1^\circ$ . (3 marks)

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5 (a) (i) Describe the geometrical transformation that maps the graph of  $y = \left(1 + \frac{x}{3}\right)^6$  onto the graph of  $y = (1 + 2x)^6$ . (2 marks)

(ii) The curve  $y = \left(1 + \frac{x}{3}\right)^6$  is translated by the vector  $\begin{bmatrix} 3 \\ 0 \end{bmatrix}$  to give the curve  $y = g(x)$ . Find an expression for  $g(x)$ , simplifying your answer. (2 marks)

(b) The first four terms in the binomial expansion of  $\left(1 + \frac{x}{3}\right)^6$  are  $1 + ax + bx^2 + cx^3$ . Find the values of the constants  $a$ ,  $b$  and  $c$ , giving your answers in their simplest form. (4 marks)

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6 An arithmetic series has first term  $a$  and common difference  $d$ .

The sum of the first 25 terms of the series is 3500.

(a) Show that  $a + 12d = 140$ . (3 marks)

(b) The fifth term of this series is 100.  
Find the value of  $d$  and the value of  $a$ . (4 marks)

(c) The  $n$ th term of this series is  $u_n$ . Given that

$$33 \left( \sum_{n=1}^{25} u_n - \sum_{n=1}^k u_n \right) = 67 \sum_{n=1}^k u_n$$

find the value of  $\sum_{n=1}^k u_n$ . (3 marks)

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**7 (a)** Sketch the graph of  $y = \frac{1}{2^x}$ , indicating the value of the intercept on the  $y$ -axis. (2 marks)

**(b)** Use logarithms to solve the equation  $\frac{1}{2^x} = \frac{5}{4}$ , giving your answer to three significant figures. (3 marks)

**(c)** Given that

$$\log_a(b^2) + 3 \log_a y = 3 + 2 \log_a \left( \frac{y}{a} \right)$$

express  $y$  in terms of  $a$  and  $b$ .

Give your answer in a form not involving logarithms. (5 marks)

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**8 (a)** Given that  $2 \sin \theta = 7 \cos \theta$ , find the value of  $\tan \theta$ . *(2 marks)*

**(b) (i)** Use an appropriate identity to show that the equation

$$6 \sin^2 x = 4 + \cos x$$

can be written as

$$6 \cos^2 x + \cos x - 2 = 0 \quad \text{(2 marks)}$$

**(ii)** Hence solve the equation  $6 \sin^2 x = 4 + \cos x$  in the interval  $0^\circ < x < 360^\circ$ , giving your answers to the nearest degree. *(6 marks)*

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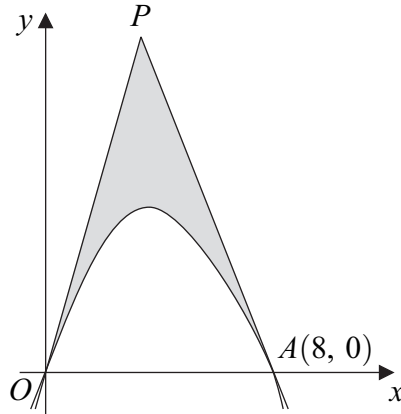






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The diagram shows part of a curve crossing the  $x$ -axis at the origin  $O$  and at the point  $A(8, 0)$ . Tangents to the curve at  $O$  and  $A$  meet at the point  $P$ , as shown in the diagram.



The curve has equation

$$y = 12x - 3x^{\frac{5}{3}}$$

- (a) Find  $\frac{dy}{dx}$ . (2 marks)
- (b) (i) Find the value of  $\frac{dy}{dx}$  at the point  $O$  and hence write down an equation of the tangent at  $O$ . (2 marks)
- (ii) Show that the equation of the tangent at  $A(8, 0)$  is  $y + 8x = 64$ . (3 marks)
- (c) Find  $\int (12x - 3x^{\frac{5}{3}}) dx$ . (3 marks)
- (d) Calculate the area of the shaded region bounded by the curve from  $O$  to  $A$  and the tangents  $OP$  and  $AP$ . (7 marks)

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Area with horizontal dotted lines for writing.

**END OF QUESTIONS**

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